

## NEW PICTURE OF PHASE EQUILIBRIA IN THE Cu-As-Se SYSTEM AND THERMODYNAMIC PROPERTIES OF TERNARY COMPOUNDS

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**Abstract.** A new complete picture of phase equilibria in the Cu-As-Se system was obtained by experimentally studying carefully crystallized alloys by prolonged thermal annealing using differential thermal analysis and powder X-ray diffraction methods, as well as considering information found in the literature. The liquidus surface projection, isothermal section at 300 K and some vertical sections of the phase diagram are presented and discussed. The types and coordinates of nonvariant and monovariant phase equilibria are determined. It is established that the liquidus surface consists of 15 regions corresponding to the primary crystallization of three initial components, seven binary and five ternary compounds. The presented phase diagram reflects the compounds  $\text{Cu}_3\text{AsSe}_4$ ,  $\text{Cu}_3\text{AsSe}_3$ ,  $\text{Cu}_7\text{As}_6\text{Se}_{13}$ ,  $\text{CuAsSe}_2$  and  $\text{CuAsSe}$ , which can be considered as synthetic analogues of natural copper-arsenic minerals. The ternary compounds  $\text{Cu}_6\text{As}_4\text{Se}_9$  and  $\text{Cu}_4\text{As}_2\text{Se}_5$ , indicated in the literature, have not been confirmed by us. The thermodynamic properties of ternary copper-arsenic selenides were studied using the EMF method with the solid electrolyte  $\text{Cu}_4\text{RbCl}_3\text{I}_2$ . From the EMF measurement data in the corresponding three-phase regions, linear equations of the temperature dependence of the EMF were obtained, from which partial thermodynamic functions of copper in the alloys were calculated. Based on these data and the solid-phase equilibrium diagram of the Cu-As-Se system, using the corresponding thermodynamic functions of copper,  $\text{As}_2\text{Se}_3$ ,  $\text{AsSe}$  and  $\text{Cu}_3\text{AsSe}_4$ , the standard Gibbs free energy of formation and the enthalpy of formation, as well as the standard entropy of the ternary compounds  $\text{Cu}_3\text{AsSe}_3$ ,  $\text{Cu}_7\text{As}_6\text{Se}_{13}$ ,  $\text{CuAsSe}_2$  and  $\text{CuAsSe}$ , were calculated.

**Key words:** phase diagram; liquidus surface projection; polythermal section; solidphase equilibria;  $\text{Cu}_2\text{Se}-\text{As}_2\text{Se}_3$  system, standard thermodynamic functions of formation,  $\text{Cu}_3\text{AsSe}_3$ ,  $\text{Cu}_7\text{As}_6\text{Se}_{13}$ ,  $\text{CuAsSe}_2$ ,  $\text{CuAsSe}$ .

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### 1. Introduction

Ternary copper chalcogenides are functional compounds due to their unique physical and chemical properties. They are widely used in many different domains, including catalysis, electronics, optoelectronics, and photoelectronics [1–8]. The results of numerous studies show the possibility of their application in alternative energy devices and other areas of high technology [9–13]. Many of these compounds have mixed ion-electron conductivity, making them very promising in developing photoelectrode materials and ion-selective sensors [14–16].

Copper-arsenic chalcogenide systems Cu-

As-X (X=S, Se) are of great interest to researchers. Ternary compounds and glassy alloys of these systems are valuable functional materials possessing semiconductor, photoelectric, optical and other practically important properties [17–25]. On the other hand, many known ternary compounds formed in Cu-As-S(Se) systems occur in nature as minerals and are of considerable interest for the study of the Earth's geochemistry [26–28]. Thus, synthetic analogues of copper minerals are used in scientific research to study and understand the properties and characteristics of these minerals,

such as their structure, thermophysical properties, magnetic properties, etc.

It is known that when developing new complex materials, information on phase equilibria and thermodynamic characteristics of the corresponding systems is of great importance, as they are the basic data for developing methods for synthesis, alloying, and growing single crystals with specified characteristics [29-31]. Earlier, in a number of works [32-44], we conducted similar comprehensive studies of complex systems based on copper chalcogenides.

In our recently published work [45], a new picture of phase equilibria in the Cu-As-S system was obtained and refined data on the standard thermodynamic functions of formation and the standard entropy of the ternary phases formed in it were obtained. This work aimed to receive a new, mutually consistent set of data on phase equilibria and thermodynamic properties of the Cu-As-Se system, which constitute the scientific basis for developing the phases formed in them.

Our analysis of the available literature data showed that the Cu-As-Se system has been studied in numerous works. However, a reliable picture of phase equilibria in this system has not been obtained to date. This concerns, first of all, data on the quasi-binary section  $\text{Cu}_2\text{Se}-\text{As}_2\text{Se}_3$ . The known versions of the T-x diagram of this section differ significantly from each other both

in the number and composition of ternary compounds, and in the temperatures and nature of their melting.

The works [46, 47] summarize the results of earlier studies (before the 1990s) of phase equilibria and characteristics of ternary phases in the Cu-As-Se system. Later, Cohen et al. [48] presented new data on phase equilibria in this system, which diverge from the already published results. In particular, the authors' phase diagram only contained the first two ternary compounds:  $\text{Cu}_3\text{AsSe}_4$ ,  $\text{CuAsSe}_2$ ,  $\text{Cu}_3\text{AsSe}_3$ , and  $\text{Cu}_6\text{As}_4\text{Se}_9$ , which were reported in the literature. Regretfully, Cohen et al. [48] did not compare their data to those from other sources.

Therefore, a comparison of the existing data reveals that no trustworthy image of phase equilibria in the Cu-As-Se system has yet to be established, even though several polythermal sections have been explored. The discrepancy in the literature data on phase equilibria of this system, in our opinion, is largely due to the tendency of alloys to glass formation and the complexity of their crystallization and achievement of an equilibrium state.

Copper-arsenic selenide crystal structure has been investigated in several publications [49-52]. Table 1 presents crystallographic data for the ternary compounds of the Cu-As-Se system indicated in the literature.

**Table 1.** Types and parameters of crystal lattices of ternary compounds of the Cu-As-Se system

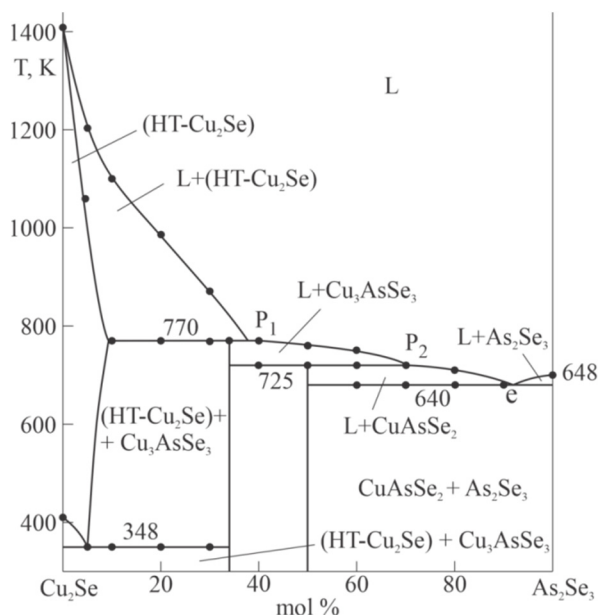
Compound	Structure, Sp.gr., lattice parameters; Å	Ref.
$\alpha\text{-Cu}_3\text{AsSe}_4$	Cubic, $a=5.535$	[49]
$\beta\text{-Cu}_3\text{AsSe}_4$	Tetragonal, $I-42m$ , $a = 5.53$ , $c = 10.83$	[49]
$\text{CuAsSe}_2$	Monoclinic, $a = 5.117$ , $b = 12.293$ , $c = 9.464$ , $\beta = 98.546$	[50]
$\text{Cu}_4\text{As}_2\text{Se}_5$	Rhombohedral, $R3$ , $a = 14.0401$ , $c = 9.6021$	[50]
$\text{Cu}_3\text{AsSe}_3$	Cubic, $Pm-3m$ , $a = 5.758$	[51]
$\text{Cu}_7\text{As}_6\text{Se}_{13}$	Hexagonal, $R3$ , $a = 14.025$ , $c = 9.61$ , $\gamma = 120$	[52]

As was indicated above, the previously presented phase diagrams of the main quasi-binary section  $\text{Cu}_2\text{Se}-\text{As}_2\text{Se}_3$  of the Cu-As-Se system are contradictory (a detailed literature analysis was conducted in [53]). Therefore, in [53] this section was re-investigated by us and its refined phase diagram was constructed. It is shown that this system is quasi-binary and is characterized by the formation of ternary compounds  $\text{Cu}_3\text{AsSe}_3$  and  $\text{CuAsSe}_2$ , which melt

with decomposition according to peritectic reactions (Fig. 1). In [53] we also have presented a new picture of phase equilibria in the  $\text{Cu}_2\text{Se}-\text{Cu}_3\text{AsSe}_4-\text{As}_2\text{Se}_3$  subsystem of the Cu-As-Se system. A projection of the liquidus surface of the  $\text{Cu}_2\text{Se}-\text{Cu}_3\text{AsSe}_4-\text{As}_2\text{Se}_3$  system, an isothermal section at 500 K, and some vertical sections of the phase diagram were constructed. The fields of primary crystallization of all seven phases of the studied system, as well as types and

coordinates of invariant and monovariant phase equilibria are determined. The presented phase diagram reflects four ternary copper-arsenic

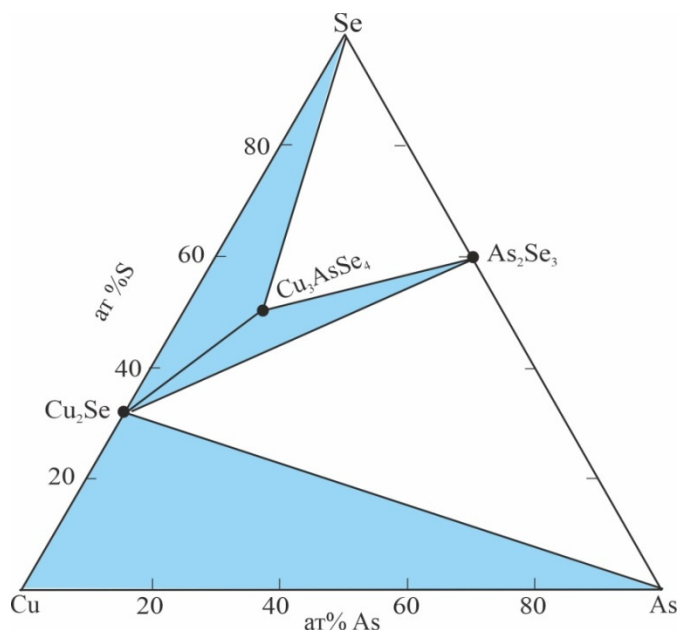
selenides  $\text{Cu}_3\text{AsSe}_4$ ,  $\text{Cu}_3\text{AsSe}_3$ ,  $\text{Cu}_7\text{As}_6\text{Se}_{13}$ , and  $\text{CuAsSe}_2$ .



**Fig. 1.** Quasi-binary system  $\text{Cu}_2\text{Se}-\text{As}_2\text{Se}_3$  [53]

Apart from the aforementioned subsystem, we have previously examined two more subsystems of the Cu-As-Se system (Fig. 2): Cu– $\text{Cu}_2\text{Se}$ –As [54] and  $\text{Cu}_2\text{Se}$ – $\text{Cu}_3\text{AsSe}_4$ –Se [55]. Using differential thermal analysis and X-ray structural analysis methods, informative graphs were constructed describing these subsystems, a

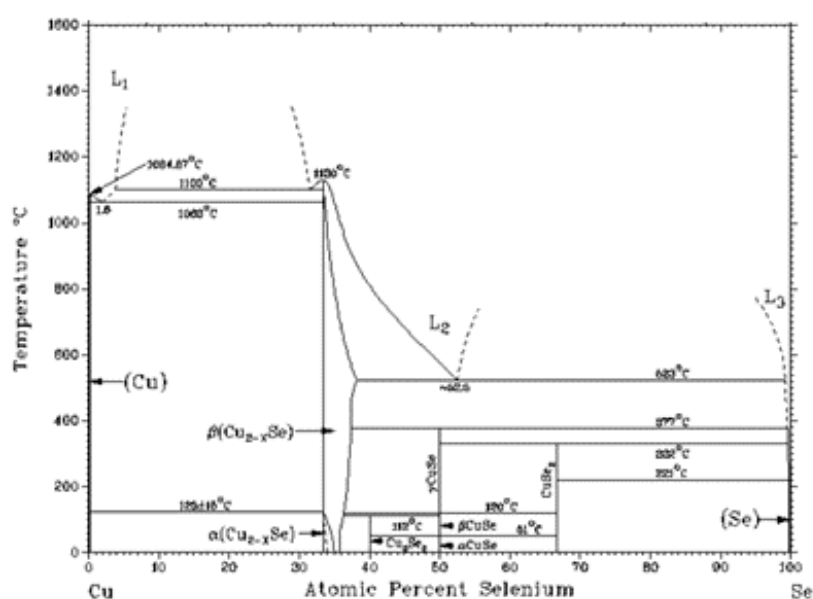
number of polythermal sections and an isothermal section of the phase diagram at 300 K, as well as a projection of the liquidus surface. Using the EMF approach with solid electrolyte, we also evaluated in [55] the standard thermodynamic functions of formation and the standard entropy of the  $\text{Cu}_3\text{AsSe}_4$  compound.



**Fig. 2.** Studied subsystems of the Cu-As-Se system [53-55]

Phase equilibria in the Cu-Se, As-Se, and Cu-As boundary binary components of the Cu-As-Se system have been thoroughly examined

and are regarded as very trustworthy [56] (Fig. 3).



CHEMICAL PROBLEMS 2025 no. 3 (23)

## 2. Experimental part

### 2.1. Starting materials

Highly pure copper granules (Cu-00029; 99.9999%), arsenic pieces (As-00004; 99.9999%), and selenium granules (Se-00002; 99.999%) from Evochem Advanced Materials GmbH (Germany) were used for synthesis.

### 2.2. Synthesis

CuSe, CuSe<sub>2</sub>, CuAs, AsSe and As<sub>2</sub>Se<sub>3</sub> binary compounds were initially synthesized by direct interaction of stoichiometric amounts of the corresponding simple substances in evacuated ( $\sim 10^{-2}$  Pa) and sealed silica ampoules. Synthesis of copper selenides was carried out in a two-zone inclined furnace. The temperature of the lower “hot” zone was 1420 K, and the upper “cold” zone was 900 K, which is slightly lower than the boiling point of selenium (958 K). Taking into account the incongruent melting of the CuSe and CuSe<sub>2</sub> compound, after the fusion of the components at  $\sim 900$  K, the ampoule was slowly cooled to 700 K, and annealed at this temperature for 500 hours. The identity of the synthesized copper selenides was verified by differential thermal analysis (DTA) and powder X-ray Diffraction (XRD) technique.

Pieces of elemental arsenic stored in an evacuated ampoule and without an oxide film were used for the synthesis of arsenic selenides. Elemental arsenic was weighed last and quickly for literally 2-3 minutes in order to minimize the likelihood of its oxidation. Arsenic selenides synthesized by fusion upon cooling solidified in the form of homogeneous glasses. Considering the difficulty of their crystallization, glassy AsSe and As<sub>2</sub>Se<sub>3</sub> were used in the preparation of Cu-As-Se alloys.

To study phase equilibria, we synthesized stoichiometric composition of the known ternary compounds (Cu<sub>3</sub>AsSe<sub>4</sub>, Cu<sub>3</sub>AsSe<sub>3</sub>, Cu<sub>7</sub>As<sub>6</sub>Se<sub>13</sub>, CuAsSe<sub>2</sub>, CuAsSe, Cu<sub>6</sub>As<sub>4</sub>Se<sub>9</sub>, Cu<sub>4</sub>As<sub>2</sub>Se<sub>5</sub>) and alloys of some isopleth sections. When preparing the alloys, we took into account the results of our previous works and focused on the Cu<sub>2</sub>Se-As<sub>2</sub>Se<sub>3</sub>-As and Cu<sub>3</sub>AsSe<sub>4</sub>-As<sub>2</sub>Se<sub>3</sub>-Se composition regions, which we had not previously considered (Fig. 2). Syntheses of ternary alloys were carried out by the interaction of pre-synthesized binary compounds and elementary components, also under vacuum conditions.

Considering the tendency of Cu-As-Se alloys

to form glasses [57, 58], when preparing samples from the region of glass formation and its surroundings, we paid special attention to the complete crystallization of glasses and achieving an equilibrium state. The cast samples obtained by cooling the melts were subjected to long-term stepwise annealing. Cast alloys prepared by fusing the initial binary and some ternary compounds, as well as a glassy alloy of stoichiometric composition As<sub>2</sub>Se<sub>3</sub> and elemental selenium, were subjected to thermal annealing at temperatures slightly below the solidus (500-600 K) for 2000-3000 h. As a result, we were able to obtain completely crystallized alloys.

### 2.3. Analysis

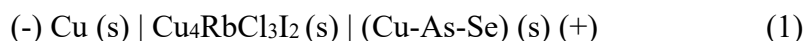
DTA and XRD techniques were employed to analyze both starting compounds and alloys. Thermal analysis of the equilibrated alloys was carried out using a NETZSCH 404 F1 Pegasus system. The DTA measurement was performed between room temperature and  $\sim 1300$  K with a heating and cooling rate of  $10 \text{ K min}^{-1}$ . The maximum heating temperature for alloys rich in arsenic and arsenic selenides did not exceed 850 K, which does not exceed their sublimation and boiling temperatures. The device was previously temperature-calibrated. For this purpose, pure metals (indium, tin, bismuth, and zinc, antimony, silver and copper) provided by NETZSCH for this purpose with the appropriate certificates were used as standards. DTA of the synthesized alloys was carried out in evacuated and sealed ampoules made of transparent quartz glass with a height of 1.5-2 cm and a diameter of 0.5 cm. The mass of the samples was in the range of 50-100 mg. The free volume of the ampoules was minimal (no more than  $0.3 \text{ cm}^3$ ), which ensured the constancy of the alloy composition during DTA measurement. Temperatures of thermal effects were taken mainly from the heating curves. NETZSCH Proteus Software was used for the evaluation of the DTA data.

The XRD analysis was performed on a Bruker D2 ADVANCE diffractometer, with CuK $\alpha_1$  radiation at room temperature. XRD patterns were indexed by using TopasV3.0 software by Bruker.

Thermodynamic studies were conducted by measuring the EMF of concentration chains of



the following type



Equilibrium alloys of the system under study were used as the right electrodes for type (1) circuits. The right electrodes were prepared by pressing annealed alloys ground into powder in the form of tablets with a diameter of ~8-10

mm and a thickness of 4-6 mm. The methodology for constructing of (1) type cells and conducting EMF measurements was similar to that in [33, 45, and 55].

### 3. Results and discussion

A complete, mutually consistent picture of phase equilibria in the Cu-As-Se system was obtained by processing the set of obtained experimental data using information from the literature on the boundary binary systems Cu-Se, Cu-As, and As-Se [56] as well as previously studied subsystems  $\text{Cu}_2\text{Se}$ - $\text{Cu}_3\text{AsSe}_4$ - $\text{As}_2\text{Se}_3$ ,  $\text{Cu}$ - $\text{Cu}_2\text{Se}$ -As, and  $\text{Cu}_2\text{Se}$ - $\text{Cu}_3\text{AsSe}_4$ -Se [53–55].

#### 3.1. Solid-phase equilibria in the Cu-As-Se system at 300 K

Solid-phase equilibria in the Cu-As-Se system were obtained in general by a joint analysis of the set of experimental data on annealed alloys, including the phase diagrams of border binary systems (Fig. 4).

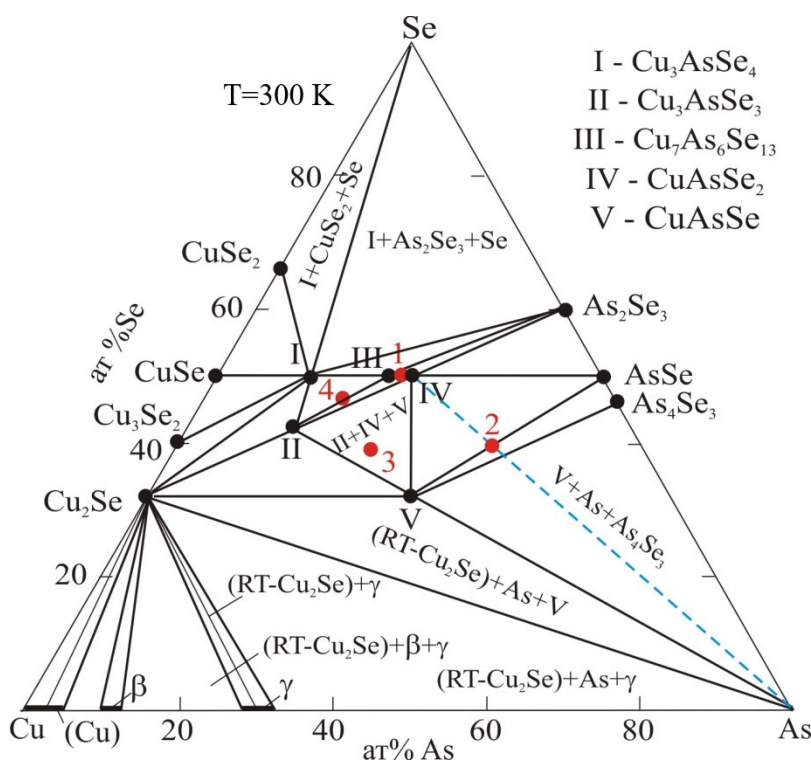


Fig. 4. Diagram of solid-phase equilibria of the Cu-As-Se system at 300 K

According to the constructed diagram, this system is characterized by the formation of 5 ternary compounds:  $\text{Cu}_3\text{AsSe}_4$ ,  $\text{Cu}_3\text{AsSe}_3$ ,  $\text{Cu}_7\text{As}_6\text{Se}_{13}$ ,  $\text{CuAsSe}_2$  and  $\text{CuAsSe}$ . Fig. 5 shows powder diffraction patterns of the indicated compounds. As can be seen, the synthesized samples of these compounds are single-phase and have diffraction patterns similar to those

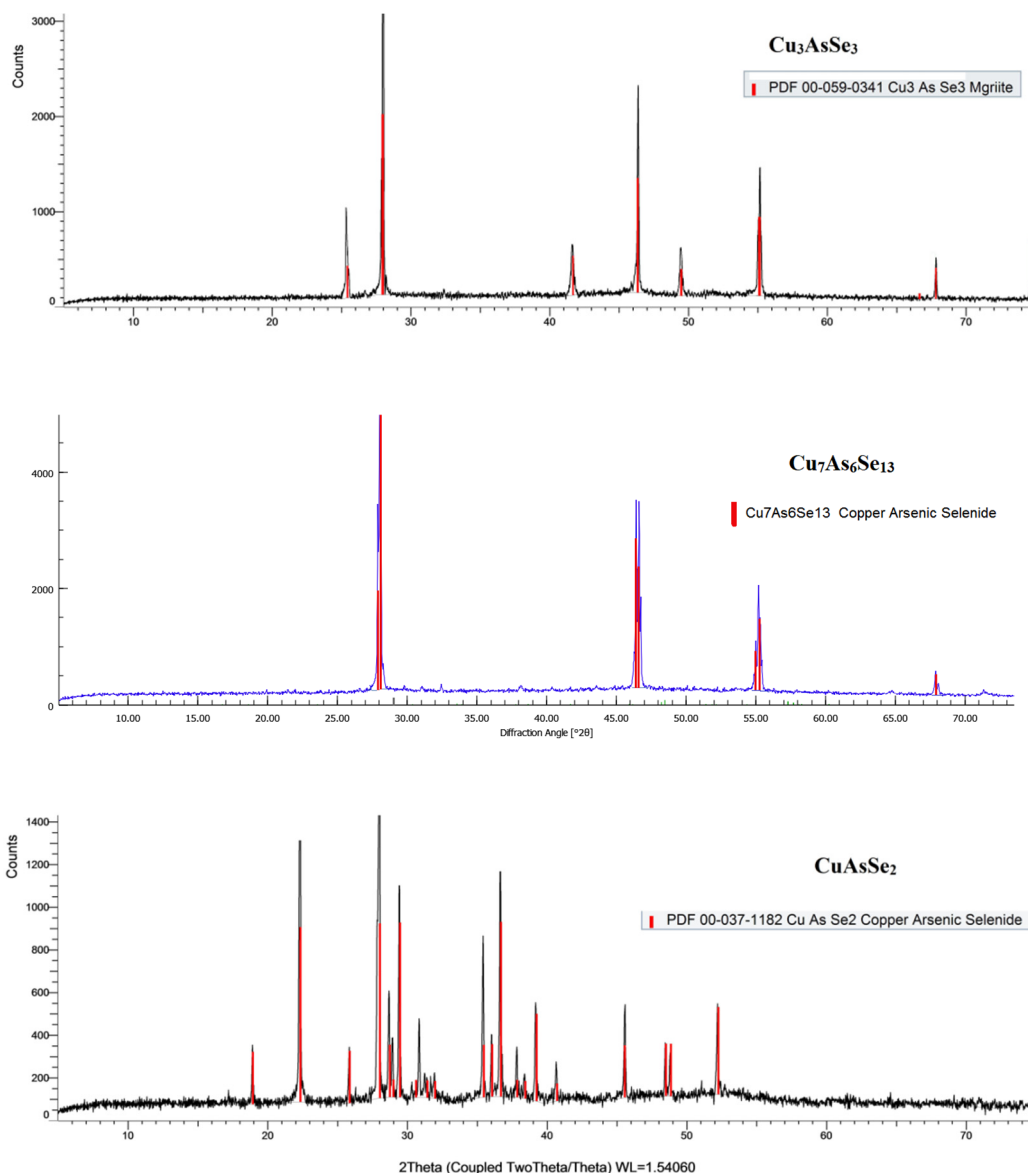
indicated in the literature [49-52]. The crystallographic data obtained from the powder diffraction patterns are presented in Table 2. A comparison of these data with those in the literature (Table 1) showed that they are in good agreement. The ternary compounds  $\text{Cu}_6\text{As}_4\text{Se}_9$  and  $\text{Cu}_4\text{As}_2\text{Se}_5$  (respectively, alloys 1 and 4 in Fig. 4) indicated in the literature have not been

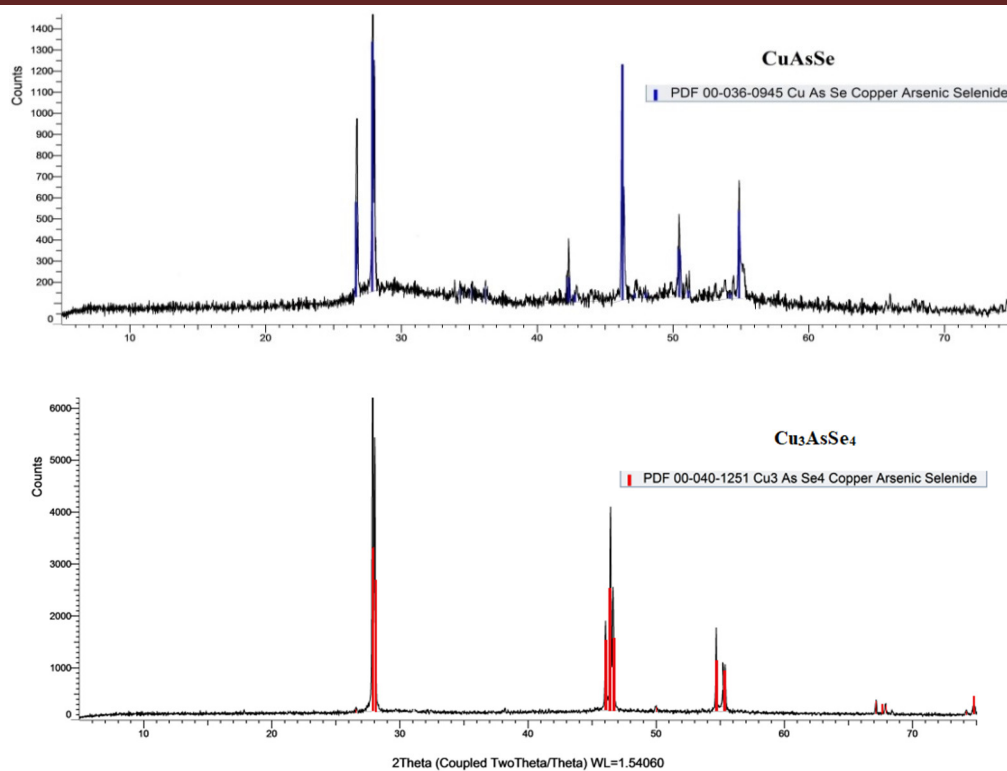
confirmed by us. Their X-ray diffraction patterns (Fig. 6) consisted of sets of reflection lines of various compounds of this system.

**Table 2.** Crystal data of ternary compounds of the Cu-As-Se system

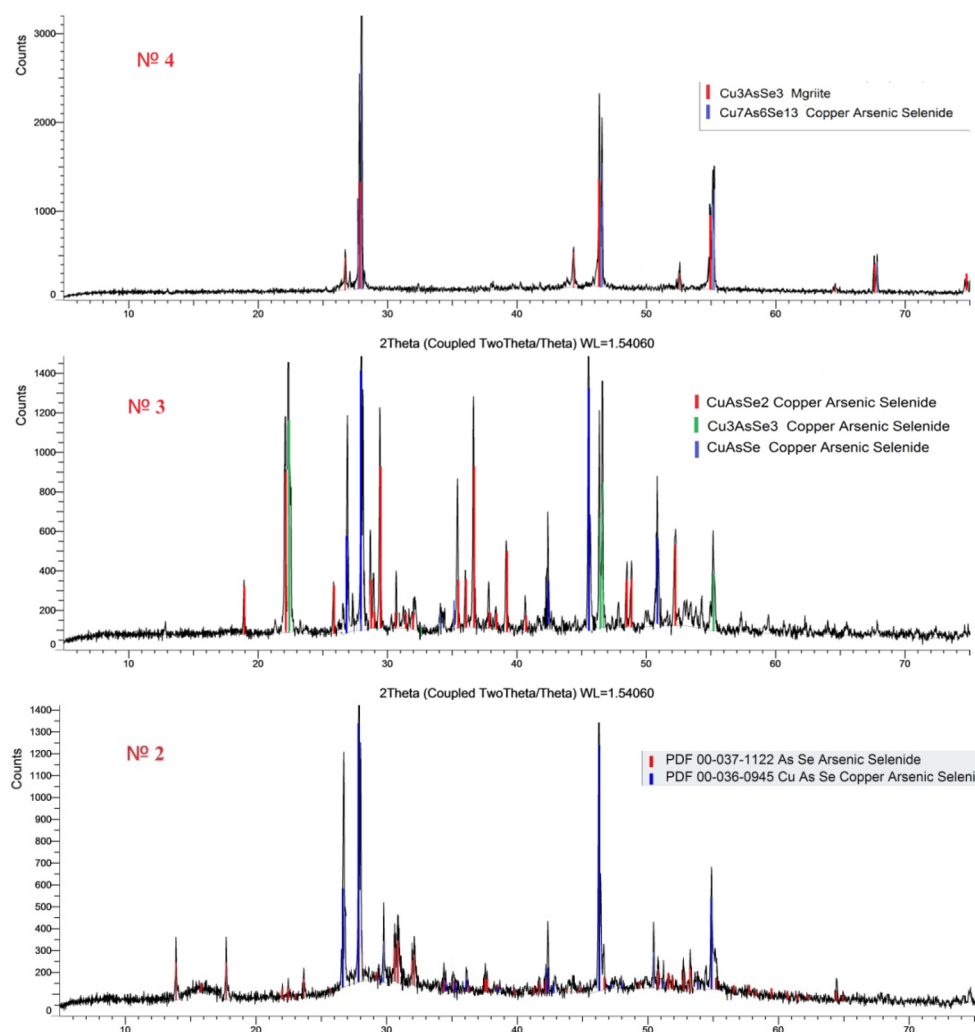
Compound	Structure, Sp.gr., lattice parameters; Å
$\alpha$ -Cu <sub>3</sub> AsSe <sub>4</sub>	Cubic, $a=5.5347$
$\beta$ -Cu <sub>3</sub> AsSe <sub>4</sub>	Tetragonal, $I-42m$ , $a = 5.5295$ , $c = 10.829$
CuAsSe <sub>2</sub>	Monoclinic, $a = 5.116$ , $b = 12.291$ , $c = 9.467$ , $\beta = 98.55^\circ$
Cu <sub>3</sub> AsSe <sub>3</sub>	Cubic, $Pm-3m$ , $a = 5.7573$
Cu <sub>7</sub> As <sub>6</sub> Se <sub>13</sub>	Hexagonal, $R3$ , $a = 14.024$ , $c = 9.613$

Fig. 4 shows the tie lines related to the studied quasi-binary sections presented by us in [53-55]. The location of other connodes and three-phase regions is clearly established by the XRD studies (Fig. 6).

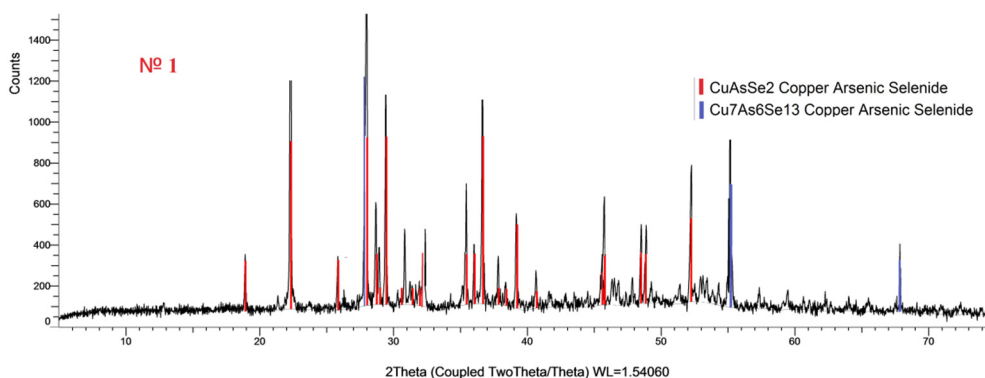




**Fig. 5.** Powder X-ray diffraction patterns of  $\text{Cu}_3\text{AsSe}_4$ ,  $\text{Cu}_3\text{AsSe}_3$ ,  $\text{Cu}_7\text{As}_6\text{Se}_{13}$ ,  $\text{CuAsSe}_2$  and  $\text{CuAsSe}$  compounds







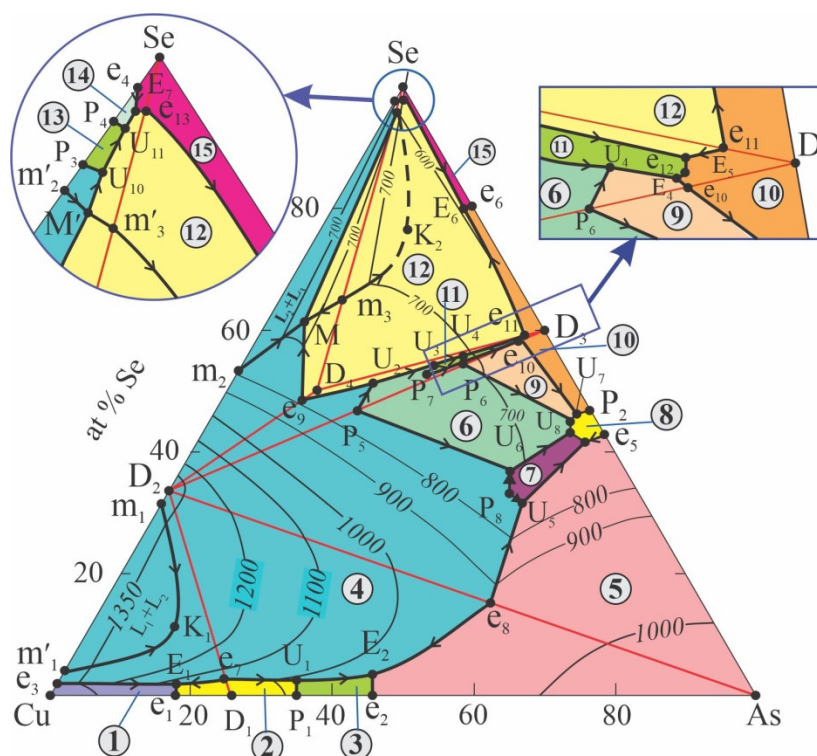
**Fig. 6.** Powder diffraction patterns of alloys 1, 2, 3, and 4 in Fig. 4

The isothermal section of the phase diagram in the region of Cu-Cu<sub>2</sub>Se-As compositions (Fig. 4) consists of two independent triangles Cu-Cu<sub>2</sub>Se- $\gamma$  and  $\gamma$ -Cu<sub>2</sub>Se-As. In this region, the presence of 3 three-phase regions delimited by tie-lines (Cu<sub>2</sub>Se)<sub>I</sub>-(Cu), (Cu<sub>2</sub>Se)<sub>I</sub>-Cu<sub>8</sub>As ( $\beta$ ) and (Cu<sub>2</sub>Se)<sub>I</sub>- $\gamma$  was established. The presence of the first two-phase region is due to the fact that up to 6 at% As of solid solutions based on Cu are formed in the

binary Cu-As system [56].

The compound (Cu<sub>2</sub>Se)<sub>I</sub> also forms concentration tie-lines with the compounds Cu<sub>3</sub>AsSe<sub>4</sub>, Cu<sub>3</sub>AsSe<sub>3</sub> and CuAsSe, as well as elemental arsenic.

In the distribution of phase regions, along with (Cu<sub>2</sub>Se)<sub>I</sub>, an important role belongs to the compounds Cu<sub>3</sub>AsSe<sub>4</sub> and CuAsSe<sub>2</sub>, which form tie-lines with the 8th and 6th phases of the system, respectively.



**Fig. 7.** Projection of the liquidus surface of the Cu-As-Se system. Fields of primary crystallization of phases: 1 - (Cu); 2 -  $\gamma$ ; 3 -  $\delta$ ; 4 - (HT-Cu<sub>2</sub>Se); 5 - As; 6 - Cu<sub>3</sub>AsSe<sub>3</sub>; 7 - CuAsSe; 8 - AsSe; 9 - CuAsSe<sub>2</sub>; 10 - As<sub>2</sub>Se<sub>3</sub>; 11 - Cu<sub>7</sub>As<sub>6</sub>Se<sub>13</sub>; 12 - Cu<sub>3</sub>AsSe<sub>4</sub>; 13 - (HT-CuSe); 14 - CuSe<sub>2</sub>; 15 - Se

**3.2. Liquidus Surface Projection.** The liquidus surface projection of the Cu-As-Se system consists of 15 fields of primary crystallization of phases (Fig. 7). Five sections

pertain to ternary copper-arsenic selenides, seven to binary compounds generated on the border systems, and three to the starting components. The fields of primary crystallization of the HT-

CuSe (P<sub>3</sub>), CuSe<sub>2</sub> (P<sub>4</sub>), and Cu<sub>7</sub>As<sub>6</sub>Se<sub>13</sub> (P<sub>7</sub>) compounds are degenerate and are shown in Fig. 7 in an enlarged form (arbitrary scale).

The crystallization surfaces of (HT-Cu<sub>2</sub>Se), As, Cu<sub>3</sub>AsSe<sub>4</sub> and Cu<sub>3</sub>AsSe<sub>3</sub> are most extended. The fields of primary crystallization (Cu), as well as  $\gamma$  (Cu<sub>3</sub>As) and  $\delta$ -phases of the binary Cu-As system extend along this side in the form of narrow stripes.

The T-x-y phase diagram of the Cu-As-Se system is characterized by the presence of two wide stratification regions L<sub>1</sub>+L<sub>2</sub> and L<sub>2</sub>+L<sub>3</sub> (L<sub>1</sub>

is a metallic melt based on Cu-As; L<sub>2</sub> is a melt based on selenides; L<sub>3</sub> is a liquid phase rich in elemental selenium), formed by the penetration (or spread) of the corresponding regions on the Cu-Se boundary system.

The fields of primary crystallization of phases are delimited by numerous curves of monovariant equilibria and points of nonvariant equilibria. The coordinates of nonvariant points and the types of corresponding equilibria are given in Table 3.

**Table 3.** Non-variant equilibria in the Cu-As-Se system

Point in Fig.7	Equilibrium	T, K
D <sub>1</sub>	L $\leftrightarrow$ $\gamma$ (Cu <sub>3</sub> As)	1100
D <sub>2</sub>	L $\leftrightarrow$ (HT-Cu <sub>2</sub> Se)	1403
D <sub>3</sub>	L $\leftrightarrow$ As <sub>2</sub> Se <sub>3</sub>	648
D <sub>4</sub>	L $\leftrightarrow$ I	750
P <sub>1</sub>	L+ $\gamma$ $\leftrightarrow$ $\delta$	982
P <sub>2</sub>	L+As <sub>2</sub> Se <sub>3</sub> $\leftrightarrow$ AsSe	570
P <sub>3</sub> *	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ (HT-CuSe)	650
P <sub>4</sub> *	L+ (HT-CuSe) $\leftrightarrow$ CuSe <sub>2</sub>	605
P <sub>5</sub>	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ II	770
P <sub>6</sub>	L+II $\leftrightarrow$ IV	725
P <sub>7</sub>	L+II $\leftrightarrow$ III	740
P <sub>8</sub>	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ V	710
e <sub>1</sub>	L $\leftrightarrow$ (Cu)+ $\gamma$	958
e <sub>2</sub>	L $\leftrightarrow$ $\delta$ +As	873
e <sub>3</sub>	L $\leftrightarrow$ (Cu)+(HT-Cu <sub>2</sub> Se)	1335
e <sub>4</sub> *	L $\leftrightarrow$ CuSe <sub>2</sub> +Se	494
e <sub>5</sub>	L $\leftrightarrow$ As+AsSe	522
e <sub>6</sub>	L $\leftrightarrow$ As <sub>2</sub> Se <sub>3</sub> +Se	420
e <sub>7</sub>	L $\leftrightarrow$ (HT-Cu <sub>2</sub> Se)+ $\gamma$	990
e <sub>8</sub>	L $\leftrightarrow$ (HT-Cu <sub>2</sub> Se)+As	925
e <sub>9</sub>	L $\leftrightarrow$ (HT-Cu <sub>2</sub> Se)+I	743
e <sub>10</sub>	L $\leftrightarrow$ IV+As <sub>2</sub> Se <sub>3</sub>	640
e <sub>11</sub>	L $\leftrightarrow$ I+As <sub>2</sub> Se <sub>3</sub>	642
e <sub>12</sub>	L $\leftrightarrow$ III+As <sub>2</sub> Se <sub>3</sub>	640
e <sub>13</sub>	L $\leftrightarrow$ I+Se	490
m <sub>1</sub> (m <sub>1</sub> ')	L <sub>2</sub> $\leftrightarrow$ L <sub>1</sub> +(HT-Cu <sub>2</sub> Se)	1373
m <sub>2</sub> (m <sub>2</sub> ')	L <sub>2</sub> $\leftrightarrow$ L <sub>3</sub> +(HT-Cu <sub>2</sub> Se)	796
m <sub>3</sub> (m <sub>3</sub> ')	L <sub>2</sub> $\leftrightarrow$ L <sub>3</sub> + I	713
U <sub>1</sub>	L+ $\gamma$ $\leftrightarrow$ (HT-Cu <sub>2</sub> Se)+ $\delta$	965
U <sub>2</sub>	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ I+II	720
U <sub>3</sub>	L+II $\leftrightarrow$ I+III	703

U <sub>4</sub>	L+II $\leftrightarrow$ III+IV	715
U <sub>5</sub>	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ V+As	705
U <sub>6</sub>	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ II+V	703
U <sub>7</sub>	L+As <sub>2</sub> Se <sub>3</sub> $\leftrightarrow$ IV+AsSe	560
U <sub>8</sub>	L+IV $\leftrightarrow$ II+AsSe	545
U <sub>9</sub>	L+II $\leftrightarrow$ V+AsSe	530
U <sub>10</sub>	L+(HT-Cu <sub>2</sub> Se) $\leftrightarrow$ I+(HT-CuSe)	630
U <sub>11</sub>	L+(HT-CuSe) $\leftrightarrow$ I+CuSe <sub>2</sub>	600
M(M')	L <sub>2</sub> $\leftrightarrow$ L <sub>3</sub> +(HT-Cu <sub>2</sub> Se)+I	690
E <sub>1</sub>	L $\leftrightarrow$ (Cu)+(HT-Cu <sub>2</sub> Se)+ $\gamma$	935
E <sub>2</sub>	L $\leftrightarrow$ (HT-Cu <sub>2</sub> Se)+As+ $\delta$	855
E <sub>3</sub>	L $\leftrightarrow$ V+AsSe+As	515
E <sub>4</sub> **	L $\leftrightarrow$ III+IV+As <sub>2</sub> Se <sub>3</sub>	635
E <sub>5</sub> **	L $\leftrightarrow$ I+III+As <sub>2</sub> Se <sub>3</sub>	637
E <sub>6</sub>	L $\leftrightarrow$ I+As <sub>2</sub> Se <sub>3</sub> +Se	415
E <sub>7</sub>	L $\leftrightarrow$ I+CuSe <sub>2</sub> +Se	490

\* - denotes equilibria degenerate at the angle Se of the concentration triangle

\*\* - denotes equilibria degenerate at the points e<sub>10</sub> and e<sub>12</sub>.

The eutectic curve emanating from point e<sub>9</sub> intersects the immiscibility region L<sub>2</sub>+L<sub>3</sub> and transforms this equilibrium into a four-phase monotectic equilibrium (conjugate points M<sub>1</sub>M<sub>1</sub>' in Fig. 7).

In conclusion of this section, we note that the liquidus surface projection of this system obtained by us experimentally has a significantly more complex picture of phase equilibria compared to the liquidus surfaces projection given by the authors [48], which reflects only two

ternary compounds Cu<sub>3</sub>AsSe<sub>4</sub> and CuAsSe<sub>2</sub>.

**3.3. Some polythermal sections. The CuSe-AsSe section** (Fig. 8) passes through the stoichiometric compositions of three ternary compounds of the Cu-As-Se system and is stable below the solidus, i.e. it does not cross three-phase regions. At high temperatures, from left to right, the section reflects the primary crystallization of the  $\alpha$ -phase, HT-Cu<sub>3</sub>AsSe<sub>4</sub>, Cu<sub>3</sub>AsSe<sub>3</sub>, CuAsSe<sub>2</sub> and As<sub>2</sub>Se<sub>3</sub>.

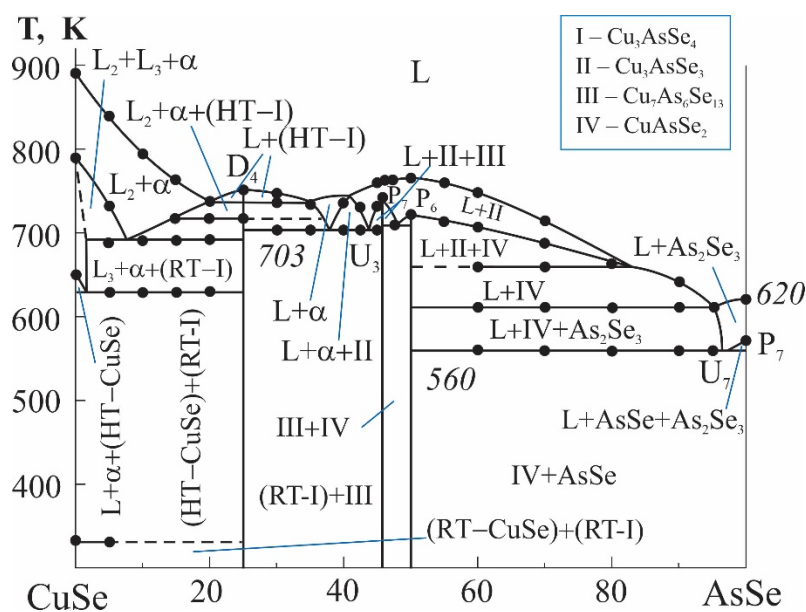


Fig. 8. Polythermal section CuSe-AsSe



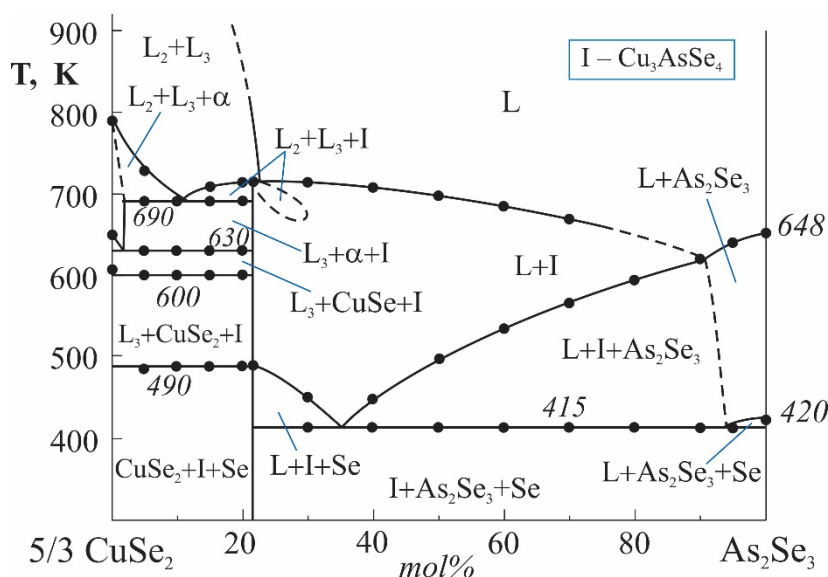


Fig. 10. Polythermal section  $\frac{5}{3}\text{CuSe}_2\text{-As}_2\text{Se}_3$

It should be noted that the polythermal sections considered and the projection of the liquidus surface as a whole reflect the processes occurring during heating of samples brought to a state as close as possible to equilibrium by means of prolonged thermal annealing. When cooling the melts of these samples, especially from the region adjacent to arsenic selenides, they solidify in the form of glass or crystal+glass mixtures.

**3.4. Thermodynamic properties of copper-arsenic selenides.** Measurements of the EMF of reversible concentration chains of type (1) for equilibrium crystalline alloys of the Cu-As-Se system from the composition range  $\text{Cu}_2\text{Se-CuAsSe-AsSe-Se}$  led to reproducible results. According to the measurement data in each of the three-phase regions  $\text{I+III+As}_2\text{Se}_3$ ,

$\text{III+IV+As}_2\text{Se}_3$ ,  $\text{I+II+III}$  and  $\text{IV+V+AsSe}$ , indicated in the solid-phase equilibrium diagram of this system (Fig. 4), at a constant temperature the EMF has constant values regardless of the overall composition of the alloys, and undergoes abrupt changes when passing from one three-phase region to another. The data of EMF measurements of chains of type (1) for alloys from the three-phase region  $\text{I+As}_2\text{Se}_3\text{+Se}$  and the processing of their results were carried out by us in [55].

Fig. 11 shows the temperature dependences of the EMF of circuits of type (1) for a number of phase regions of the Cu-As-Se system. As can be seen, all these dependences are linear and can be used in thermodynamic calculations.

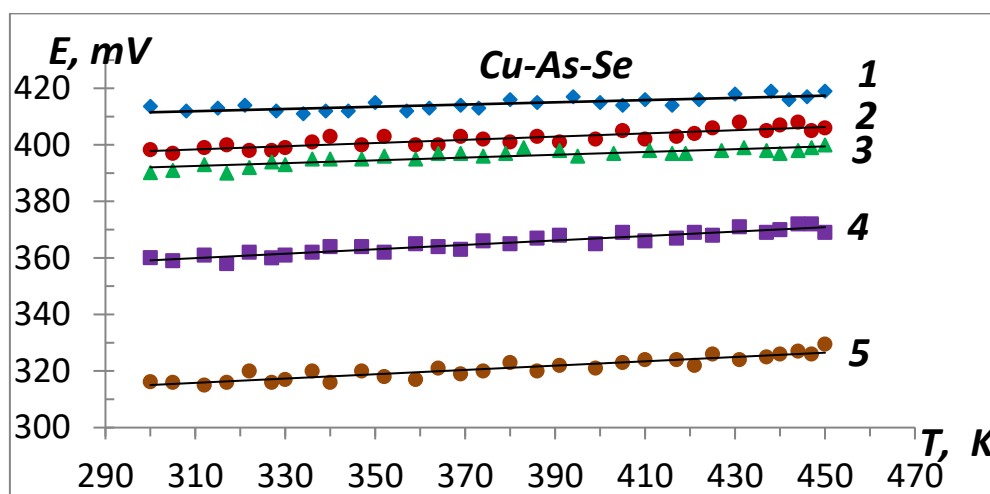


Fig. 11. Temperature dependences of the EMF of (1) type cells for alloys from phase areas  $\text{I+As}_2\text{Se}_3\text{+Se}$  (1) [55],  $\text{I+III+As}_2\text{Se}_3$  (2),  $\text{III+IV+As}_2\text{Se}_3$  (3),  $\text{I+II+III}$  (4) и  $\text{IV+V+AsSe}$  (5) of the Cu-As-Se system



For thermodynamic calculations, the results of EMF measurements in these phase regions were processed using the least squares

method and linear equations of the type below were obtained

$$E = a + bT \pm t \left[ \frac{S_E^2}{n} + S_b^2 (T_i - \bar{T})^2 \right]^{1/2}$$

Obtained equations are presented in Table 4. From the data in Table 4, the relative partial thermodynamic functions of copper in alloys at

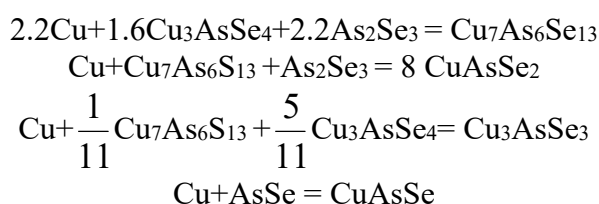
298 K were calculated using known thermodynamic relationships (Table 5).

**Table 4.** Temperature dependences of the EMF of chains of type (1) in some phase regions of the Cu-As-Se system (T=300-450K)

The phase region in Fig. 4	$E, mB = a + bT \pm 2S_E(T)$
I+III+As <sub>2</sub> Se <sub>3</sub>	$382,92 + 0,0513T \pm 2 \left[ \frac{3,9}{30} + 6.2 \cdot 10^{-5} (T - 376,8)^2 \right]^{1/2}$
III+IV+As <sub>2</sub> Se <sub>3</sub>	$370.73 + 0,0652T \pm 2 \left[ \frac{2,4}{30} + 3.9 \cdot 10^{-5} (T - 376.2)^2 \right]^{1/2}$
I+II+III	$341.79 + 0,0601T \pm 2 \left[ \frac{2,7}{30} + 4.2 \cdot 10^{-5} (T - 375.3)^2 \right]^{1/2}$
IV+V+AsSe	$289.92 + 0,0879T \pm 2 \left[ \frac{3,2}{30} + 5.1 \cdot 10^{-5} (T - 376.2)^2 \right]^{1/2}$

According to the solid-phase equilibrium diagram of the Cu-As-Se system (Fig. 4), the values of partial molar quantities in the above-mentioned three-phase regions are

thermodynamic characteristics of the following potential-forming reactions (all substances are crystalline):



According to the equations of these reactions, the standard thermodynamic functions of formation and the standard entropies of

copper-arsenic selenides can be calculated using the following relationships ( $\Delta Z \equiv \Delta G$  or  $\Delta H$ ):

$$\begin{aligned} \Delta Z_{\text{Cu}_7\text{As}_6\text{Se}_{13}}^0 &= 2.2\Delta \bar{Z}_{\text{Cu}} + 1.6\Delta Z_{\text{Cu}_3\text{AsSe}_4}^0 + 2.2\Delta Z_{\text{As}_2\text{Se}_3}^0 \\ \Delta Z_{\text{CuAsSe}_2}^0 &= 0.125\Delta \bar{Z}_{\text{Cu}} + 0.125\Delta Z_{\text{Cu}_7\text{As}_6\text{Se}_{13}}^0 + 0.125\Delta Z_{\text{As}_2\text{Se}_3}^0 \\ \Delta Z_{\text{Cu}_3\text{AsSe}_3}^0 &= \Delta \bar{Z}_{\text{Cu}} + \frac{1}{11}\Delta Z_{\text{Cu}_7\text{As}_6\text{Se}_{13}}^0 + \frac{5}{11}\Delta Z_{\text{Cu}_3\text{AsSe}_4}^0 \\ \Delta Z_{\text{CuAsSe}}^0 &= \Delta \bar{Z}_{\text{Cu}} + \Delta Z_{\text{AsSe}}^0 \end{aligned}$$

and the standard entropies:

$$S_{\text{Cu}_7\text{As}_6\text{Se}_{13}}^0 = 2.2(\Delta \bar{S}_{\text{Cu}} + S_{\text{Cu}}^0) + 1.6S_{\text{Cu}_3\text{AsSe}_4}^0 + 2.2S_{\text{As}_2\text{Se}_3}^0$$



$$S_{\text{CuAsSe}_2}^0 = 0.125(\Delta \bar{S}_{\text{Cu}} + S_{\text{Cu}}^0) + 0.125S_{\text{Cu}_7\text{As}_6\text{Se}_{13}}^0 + 0.125S_{\text{As}_2\text{Se}_3}^0$$

$$S_{\text{Cu}_3\text{AsSe}_3}^0 = \Delta \bar{S}_{\text{Cu}} + S_{\text{Cu}}^0 + \frac{1}{11}S_{\text{Cu}_7\text{As}_6\text{Se}_{13}}^0 + \frac{5}{11}S_{\text{Cu}_3\text{AsSe}_4}^0$$

$$S_{\text{CuAsSe}}^0 = \Delta \bar{S}_{\text{Cu}} + S_{\text{Cu}}^0 + S_{\text{AsSe}}^0$$

**Table 5.** Partial molar functions of copper in Cu-As-Se alloys at 298K

Phase area	$-\Delta \bar{G}_{\text{Cu}}$	$-\Delta \bar{H}_{\text{Cu}}$	$-\Delta \bar{S}_{\text{Cu}},$ $\text{J}\cdot\text{K}^{-1}\cdot\text{mole}^{-1}$
	$\text{kJ}\cdot\text{mole}^{-1}$		
I+III+As <sub>2</sub> Se <sub>3</sub>	38,42±0,07	36,95±0,29	4,95±0,76
III+IV+As <sub>2</sub> Se <sub>3</sub>	37,65±0,05	35,77±0,23	6,29±0,61
I+II+III	34,71±0,06	32,98±0,24	5,80±0,64
IV+V+AsSe	30,50±0,06	27,97±0,26	8,48 ±0,69

In addition to our own experimental results (Table 4), the calculations used the values of the standard entropies of copper ( $33.15 \pm 0.08 \text{ J}\cdot\text{K}^{-1}\cdot\text{mole}^{-1}$ ) and selenium ( $42.13 \pm 2.09 \text{ J}\cdot\text{K}^{-1}\cdot\text{mole}^{-1}$ ) [59], as well as mutually consistent data sets for As<sub>2</sub>Se<sub>3</sub> and AsSe (Table 5) [60].

**Table 5.** Standard thermodynamic functions of formation and standard entropies of ternary phases of the Cu-As-Se system

Compound	$-\Delta_f G^\circ (298 \text{ K})$	$-\Delta_f H^\circ (298 \text{ K})$	$S^\circ (298 \text{ K})$ $\text{J}\cdot\text{K}^{-1}\cdot\text{mole}^{-1}$
	$\text{kJ}\cdot\text{mole}^{-1}$		
As <sub>2</sub> Se <sub>3</sub> [60]	55,26±0,58	59,4±3,9	184,4±8,2
AsSe [60]	24,64±0,25	27,61±1,7	68,1±3,9
Cu <sub>3</sub> AsSe <sub>4</sub> [55]	147.3±0.5	146.3±1.5	307±13
Cu <sub>7</sub> As <sub>6</sub> Se <sub>13</sub>	441,8±2,3	446,1±11,7	970±27
CuAsSe <sub>2</sub>	61.1±0.4	62.1±1.9	149.5±4.5
Cu <sub>3</sub> AsSe <sub>3</sub>	141,8±0,5	140,0±2,0	258,5±5,6
CuAsSe	55,1±0,3	55,6±2,0	109,5±4,7

Thus, using the EMF method with a Cu+-conducting solid electrolyte, new sets of thermodynamic data for copper-arsenic selenides were obtained, including the partial molar Gibbs free energy of formation, the enthalpy and

entropy of copper in alloys and the corresponding standard thermodynamic functions of formation and standard entropies of ternary copper-arsenic selenides.

#### 4. Conclusions

1. By employing powder X-ray diffraction and differential thermal analysis techniques to investigate carefully formed alloys by lengthy thermal annealing, along with information from the literature, a novel comprehensive picture of phase equilibria in the Cu-As-Se system was obtained.
2. We present and analyze the liquidus surface projection, the isothermal section at 300 K, and a few vertical phase diagram sections. The types and coordinates of monovariant and nonvariant phase equilibria were established.
3. It is established that the liquidus surface consists of 15 regions corresponding to the primary crystallization of three initial components, seven binary and five ternary compounds Cu<sub>3</sub>AsSe<sub>4</sub>, Cu<sub>3</sub>AsSe<sub>3</sub>, Cu<sub>7</sub>As<sub>6</sub>Se<sub>13</sub>, CuAsSe<sub>2</sub> and CuAsSe.

4. The ternary compounds  $\text{Cu}_6\text{As}_4\text{Se}_9$  and  $\text{Cu}_4\text{As}_2\text{Se}_5$ , indicated in the literature, have not been confirmed by us.
5. By measuring the EMF of the concentration circuits relative to the copper electrode and taking into account the diagram of solid-phase

equilibria of the Cu-As-Se system, mutually consistent values of the standard thermodynamic functions of formation and standard entropies of the above-mentioned copper-arsenic selenides were obtained.

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